Algebra, Section R. 7

A linear equation in one variable is an equation that is equivalent to one of the form $a x+b=0$, where $a$ and $b$ are real numbers and $a \neq 0$.

A quadratic equation is an equation that is equivalent to one of the form $a x^{2}+b x+c=0$, where $a, b$, and $c$ are real numbers and $a \neq 0$.

## Equation-Solving Principles

For any real numbers $a, b$, and $c$,
The Addition Principle: If $a=b$ is true, then $a+c=b+c$ is true.
The Multiplication Principle: If $a=b$ is true, then $a c=b c$ is true.
The Principle of Zero Products: If $a b=0$ is true, then $a=0$ or $b=0$, and if $a=0$ or $b=0$, then $a b=0$.
The Principle of Square Roots: If $x^{2}=k$, then $x=\sqrt{k}$ or $x=-\sqrt{k}$.

Solve:

1. $6 x-15=45$
2. $5 x-10=45$
3. $9 t+4=-5$
4. $3 m-7=-13+m$
5. $11-3 x=5 x+3$
6. $2(x+7)=5 x+14$
7. $x^{2}-8 x=0$
8. $y^{2}+6 y+9=0$
9. $x^{2}+100=20 x$
10. $14=x(x-5)$
11. $x^{2}-36=0$
12. $z^{2}=144$
13. $2 x^{2}-20=0$
14. $3[5-3(4-t)]-2=5[3(5 t-4)+8]-26$
15. $x-\{3 x-[2 x-(5 x-(7 x-1))]\}=x+7$

## Exercise Set R. 7

1. 10
2. 11
3. -1
4. -12
5. 2 11. -1
6. $\frac{18}{5}$
$\begin{array}{llllll}15 .-3 & 17.1 & 19.0 & \text { 21. }-\frac{1}{10} & 23.5 & 25 .-\frac{3}{2}\end{array}$
7. $\frac{20}{7}$
$\begin{array}{lll}\text { 29. }-7,4 & 31.0,8 & \text { 33. }-3\end{array}$
8. 10
9. $-4,8$
10. $-2,-\frac{2}{3}$
11. $-\frac{3}{4}, \frac{2}{3}$
12. $-\frac{4}{3}, \frac{7}{4}$
13. $-2,7$
14. $-6,6$
15. $-12,12$
16. $-\sqrt{10}, \sqrt{10}$
17. $-\sqrt{3}, \sqrt{3}$
18. Discussion and Writing 57. $\frac{23}{66}$
59.8
19. $-\frac{6}{5},-\frac{1}{4}, 0, \frac{2}{3}$
20. $-3,-2,3$
